



Memorandum

To: All Fellows, Affiliates, Associates and Correspondents of the Canadian Institute of Actuaries and Other Interested Parties

From: Jim Christie, Chair
Actuarial Standards Board
Ty Faulds, Chair
Designated Group

Date: May 15, 2014

Subject: **Final Communication of Promulgations of the Maximum Net Credit Spread, Ultimate Reinvestment Rates, and Calibration Criteria for Stochastic Risk-Free Interest Rates in the Standards of Practice for the Valuation of Insurance Contract Liabilities: Life and Health (Accident and Sickness) Insurance (Subsection 2330 of the Final Standards for Revisions to the Standards of Practice)**

Document 214046

1. INTRODUCTION

Subsection 2330 of the Final Standard - Revisions to Economic Reinvestment Assumptions within the Practice-Specific Standards of Practice on Insurance Contract Valuation: Life and Health (Accident and Sickness) Insurance (Section 2300 and Subsection 1110), published concurrently, refers to a number of economic parameters that would be promulgated from time to time by the Actuarial Standards Board (ASB). These economic parameters are the maximum net credit spread, the ultimate reinvestment rates (URRs), and the calibration criteria for stochastic risk-free interest rates.

The ASB appointed the same designated group that is responsible for developing revised standards of practice, as described in the cover memo to the Final Standard, to develop these related promulgations.

An [Initial Communication of Promulgations](#) of the maximum net credit spread, ultimate reinvestment rates, and calibration criteria for stochastic risk-free interest rates was published on December 13, 2013, concurrent with the [Exposure Draft](#) – Revisions to Economic Reinvestment Assumptions within the Practice-Specific Standards of Practice on Insurance Contract Valuation: Life and Health (Accident and Sickness) Insurance

(Section 2300 and Subsection 1110), with a comment period ending February 14, 2014. No comments were received on the Initial Communication.

The Promulgations are the same as those proposed in the Initial Communication.

The ASB intends to review these promulgations every five years, or sooner if circumstances warrant.

2. PROMULGATION OF THE MAXIMUM NET CREDIT SPREAD

2.1. Background

Paragraph 2330.07.1 includes a reference to a maximum for the difference between the asset's credit spread and its asset depreciation assumption (the "maximum net credit spread") for assets purchased on or after the 30th anniversary from the balance sheet date:

.07.1 In all scenarios other than the base scenario, credit spreads include margins for adverse deviations as described in paragraph 2340.10.3. The actuary would also include an additional provision for adverse deviations by modifying the assumptions, if needed, on each fixed income asset purchased or sold on or after the 5th anniversary from the balance sheet date, such that

for assets purchased or sold on or after the 30th anniversary from the balance sheet date, the difference between the asset's credit spread and its asset depreciation assumption is not larger than a maximum promulgated from time to time by the Actuarial Standards Board; and

for assets purchased or sold between the 5th and 30th anniversary from the balance sheet date, the difference between the asset's credit spread and its asset depreciation assumption is not larger than using a uniform transition between the corresponding difference if purchased on the 5th anniversary from the balance sheet date and the promulgated maximum if purchased on the 30th anniversary from the balance sheet date.

2.2. Promulgation

The promulgated maximum for the difference between the asset's credit spread and its asset depreciation assumption for assets purchased on or after the 30th anniversary from the balance sheet date shall be equal to 80 basis points.

2.3. Rationale

The maximum net credit spread was developed using the following approach:

- i. The average historical credit spread was calculated for short, medium, and long corporate bonds of various credit ratings over an extended historical period (of at least 25 years);
- ii. These credit spreads were adjusted by the average best estimate asset depreciation assumption from current industry practice;
- iii. These best estimate credit spreads net of default were adjusted by the margin for adverse deviations of 10% from paragraph 2340.10.3; and
- iv. The maximum credit spread of 80 basis points was developed assuming a representative mix of corporate bonds (higher weighting of A-rated bonds) of short, medium, and long durations (higher weighting of long-duration bonds).

3. PROMULGATION OF ULTIMATE REINVESTMENT RATES

3.1. Background

Paragraph 2330.09.01 includes a reference to ultimate risk-free reinvestment rates that are used in the construction of the base and prescribed scenarios:

.09.01 The Actuarial Standards Board will promulgate from time to time the following ultimate risk-free reinvestment rates for use in the base scenario and the prescribed scenarios:

- short-term ultimate risk-free reinvestment rate-high,
- long-term ultimate risk-free reinvestment rate-high,
- short-term ultimate risk-free reinvestment rate-median,
- long-term ultimate risk-free reinvestment rate-median,
- short-term ultimate risk-free reinvestment rate-low, and
- long-term ultimate risk-free reinvestment rate-low.

3.2. Promulgation

The promulgated ultimate risk-free reinvestment rates to be used in the base scenario and in the prescribed scenarios are as follows:

- The short-term ultimate risk-free reinvestment rate-high shall be 10.0%;
- The long-term ultimate risk-free reinvestment rate-high shall be 10.4%;
- The short-term ultimate risk-free reinvestment rate-median shall be 4.0%;
- The long-term ultimate risk-free reinvestment rate-median shall be 5.3%;
- The short-term ultimate risk-free reinvestment rate-low shall be 1.4%; and
- The long-term ultimate risk-free reinvestment rate-low shall be 3.3%.

3.3. Rationale

The ultimate risk-free reinvestment rates in this promulgation were developed with the support of extensive testing, to be reasonably consistent with the range of risk-free interest rates that would be generated by a stochastic model that satisfies the promulgated calibration criteria for stochastic risk-free interest rates, also outlined in this document. The URR-median short-term and long-term rates were set equal to the median value (rounded to the nearest 10 basis points) of observed historical one-year maturity and 20-year maturity yields respectively. The URR-low and URR-high rates were set using the distribution of yields generated by a stochastic model that satisfies the promulgated calibration criteria. The distributions were assessed 60 years from the projection starting point, and the selected URR-low and URR-high rates were set to approximate the average of the lowest and highest 30% of observed risk-free interest rates in the stochastic projections respectively.

4. PROMULGATION OF CALIBRATION CRITERIA FOR STOCHASTIC RISK-FREE INTEREST RATES

4.1. Background

Paragraph 2330.32 includes a reference to calibration criteria for stochastic risk-free interest rates that would be met when the selection of risk-free interest rate scenarios is stochastic:

.32 If the selection of interest rate scenarios is stochastic, the actuary's calibration of stochastic models would meet the criteria for risk-free interest rates as promulgated from time to time by the Actuarial Standards Board.

4.2. Promulgation

Promulgated calibration criteria are provided for:

1. The left and right tail, and the mean reversion of the long-term risk-free interest rate;
2. The left and right tail of the short-term risk-free interest rate; and
3. The slope of the risk-free interest rates curve.

All calibration criteria are expressed as bond equivalent yields.

Calibration for the Long-Term Risk-Free Interest Rate

The long-term risk-free rate is assumed to be a term of 20 years or greater.

Left- and right-tail calibration criteria for the long-term risk-free interest rate are provided for the two-year, 10-year, and 60-year horizons. Risk-free interest rate scenarios at the two-year and 10-year horizons are influenced by the initial starting risk-free interest rate, so calibration criteria at each of a 4.00%, 6.25%, and 9.00% starting long-term risk-free interest rate are provided. At the 60-year horizon, the impact of the starting rate is assumed to be minimal, so only calibration criteria at a single starting rate of 6.25% are provided.

The following table shows the left- and right-tail criteria for the long-term risk-free interest rate.

Calibration Criteria for the Long-Term Risk-Free Interest Rate (≥ 20 -Year Maturity)

Horizon		Two-Year			10-Year			60-Year
Initial Rate		4.00%	6.25%	9.00%	4.00%	6.25%	9.00%	6.25%
Left-Tail Percentile	2.5 th	2.85%	4.25%	6.20%	2.30%	2.90%	3.65%	2.60%
	5.0 th	3.00%	4.50%	6.60%	2.50%	3.20%	4.25%	2.80%
	10.0 th	3.25%	4.80%	7.05%	2.85%	3.65%	4.95%	3.00%
Right-Tail Percentile	90.0 th	5.15%	7.80%	10.60%	6.85%	9.35%	11.60%	10.00%
	95.0 th	5.55%	8.30%	11.20%	7.85%	10.40%	12.80%	12.00%
	97.5 th	5.85%	8.70%	11.70%	8.85%	11.40%	13.90%	13.50%

These calibration criteria would be satisfied if the stochastic risk-free interest rate model produces results that are less than or equal to each of the left-tail calibration criteria, and greater than or equal to each of the right-tail calibration criteria, for each of the initial rates.

For all stochastic long-term risk-free interest rate models, the period of mean reversion would not be less than 14.5 years. The period of mean reversion is also referred to as the time constant. In a model with an explicit mean reversion speed of a , the period of the mean reversion is equal to $1/a$. For simple stochastic risk-free interest rate models with an explicit mean reversion factor, this requirement can be satisfied by considering the value of the mean reversion parameter

directly. For more complex models, this requirement can be satisfied by using a mathematical proof or using the procedure in Appendix A.

Calibration for the Short-Term Risk-Free Interest Rate

The short-term risk-free interest rate is assumed to be the one-year term.

Left and right-tail calibration criteria for the short-term risk-free interest rate are provided for the two-year and 60-year horizons. Interest rate scenarios at the two-year horizon are influenced by the initial starting interest rate, so calibration criteria at each of a 2.00%, 4.50%, and 8.00% starting short-term risk-free interest rate are provided. At the 60-year horizon, the impact of the starting risk-free interest rate is assumed to be minimal, so only calibration criteria at a single starting risk-free interest rate of 4.50% are provided.

The following table shows the left- and right-tail criteria for the short-term risk-free interest rate.

Calibration Criteria for the Short-Term Risk-Free Rate (One-Year Maturity)

Horizon		Two-Year			60-Year
Initial Rate		2.00%	4.50%	8.00%	4.50%
Left-Tail Percentile	2.5 th	0.85%	2.35%	5.50%	0.80%
	5.0 th	1.00%	2.70%	5.95%	0.90%
	10.0 th	1.15%	3.10%	6.40%	1.00%
Right-Tail Percentile	90.0 th	3.00%	5.90%	9.75%	10.00%
	95.0 th	3.35%	6.30%	10.25%	12.00%
	97.5 th	3.60%	6.65%	10.65%	13.50%

These calibration criteria would be satisfied if the stochastic risk-free interest rate model produces results that are less than or equal to each of the left-tail calibration criteria, and greater than or equal to each of the right-tail calibration criteria, for each of the initial risk-free interest rates.

Calibration for the Slope of the Risk-Free Interest Rates Curve

The slope of the yield curve is defined as the long-term risk-free interest rate less the short-term risk-free interest rate. Calibration criteria for the slope are provided for the 60-year horizon.

The following table show the criteria for the slope of the risk-free interest rates curve.

60-Year Slope Calibration Criteria

Percentile	Calibration Criteria
5 th	-1.00%
10 th	-0.25%
90 th	2.50%
95 th	3.00%

These calibration criteria will be satisfied if the distribution of the slope values produced by the model at the 60-year horizon are less than or equal to each of the left-tail calibration criteria and are greater than or equal to each of the right-tail calibration criteria.

4.3. Rationale

A [research paper](#) was released on December 21, 2013 by the Canadian Institute of Actuaries (CIA) Committee on Life Insurance Financial Reporting that provides the basis for the promulgated calibration criteria for stochastic risk-free interest rates. As noted in the research paper, models that satisfy the calibration criteria will be appropriate for use when actual risk-free interest rates are lower than the reference initial risk-free interest rates used for the calibration criteria (which were selected for consistency with the previous research paper published on the calibration of the long-term risk-free interest rate).

5. DUE PROCESS

Due process was followed in developing this promulgation document, as described in section D of the ASB's Policy on Due Process for the Adoption of Standards of Practice.

EFFECTIVE DATE AND EARLY IMPLEMENTATION

This promulgation and the associated standards are effective on October 15, 2014. Early implementation is not permitted.

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APPENDIX A

Satisfaction of the mean reversion criterion can be demonstrated with the following procedure:

1. Sort Scenarios for lowest to highest long-term rate at projection year T_0 , where T_0 is sufficiently long to accumulate substantial dispersion in rates, but not so long as to be beyond most expected reinvestments. For a typical long-term guaranteed block, T_0 might be in the range of five to 10 years.
2. Group the scenarios by rate quartile at T_0 , from lowest (Quartile 1) to highest (Quartile 4). Calculate the magnitude of dispersion of low-rate scenarios from central scenarios dispersion (T_0) = Average rate (T_0) within Quartile 1 – average rate (T_0) within combined (Quartile 2 & Quartile 3).
3. Using the same scenario grouping (ranked at T_0 , *not* re-ranked at T_0+10) calculate 10-year-later dispersion (T_0+10 , ranked T_0) = Average rate (T_0+10) within Quartile 1 – average rate (T_0+10) within combined (Quartile 2 & Quartile 3).
4. The mean reversion criterion over the projection period from T_0 to $T_0 +10$ is satisfied if dispersion (T_0+10 , ranked T_0) $\geq 0.5 * \text{dispersion } (T_0)$.
5. If the actuary can demonstrate that the model rate of mean reversion is similarly robust across other projection periods, this single test would be sufficient. If not, the test would be repeated across sufficient financially meaningful periods to demonstrate sustained periods of low rates.
6. Should periods of sustained high rates be financially stressful for a particular application in the opinion of the actuary, the demonstration would be repeated for these rates (Quartile 4 relative to quartiles 2 & 3).